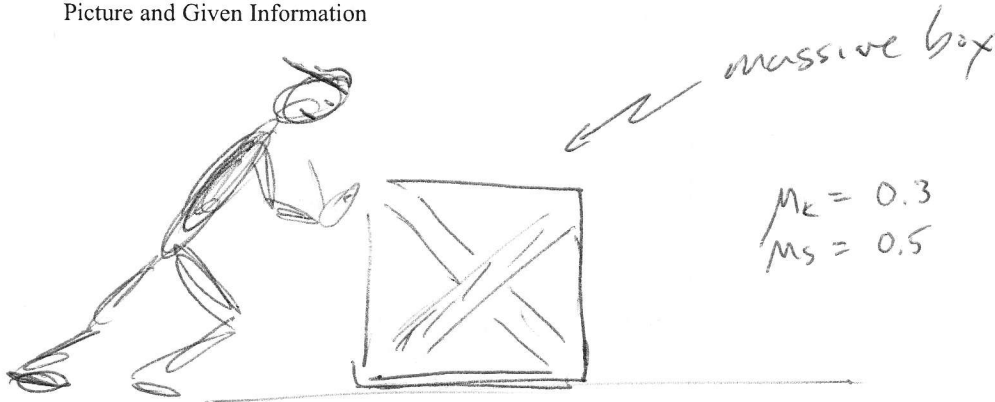


## Problem Solving Guidelines

### FOCUS the PROBLEM

Picture and Given Information



$$\begin{aligned} \mu_k &= 0.3 \\ \mu_s &= 0.5 \end{aligned}$$

$$\begin{aligned} m &= 70 \text{ kg} \\ \theta &= 50^\circ \end{aligned}$$

Question(s)

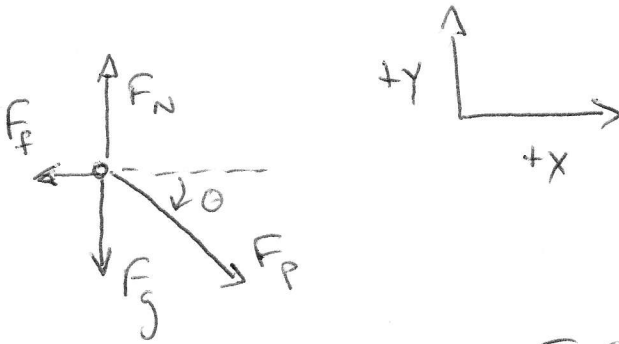
Find Force (min) needed to keep box moving.

Approach

$$\Sigma F = ma \quad \text{constant velocity means } a = 0$$

### DESCRIBE the PHYSICS

Schematic Diagram(s) (Free Body Diagrams) and Define Variable Quantities



Target Quantity(ies)

$$F_P$$

Quantitative Relationships

$$\Sigma \vec{F} = m\vec{a}$$

$$F_f = \mu F_N$$

$$v = v_0 + at$$

$$F_g = mg$$

Trig relationships

$$F_{Px} = F_P \cos \theta$$

$$F_{Py} = F_P \sin \theta$$

$$X: F_P \cos \theta - F_f = ma_x = 0$$

$$Y: F_N - F_g - F_P \sin \theta = ma_y = 0$$

$$F_f = \mu_k F_N \quad \text{use kinetic coef. since box is moving}$$

PLAN the SOLUTION

eq num

unknown

$$F_N = F_g + F_p \sin \theta$$

$$F_f = \mu_k F_N = \mu_k F_g + \mu_k F_p \sin \theta$$

$$F_p \cos \theta - \mu_k F_g - \mu_k F_p \sin \theta = 0$$

$$F_p (\cos \theta - \mu_k \sin \theta) = \mu_k F_g$$

Sufficient equations?

Yup - 3 equations and 3 unknowns


Work to target

$$F_p = \frac{\mu_k m g}{(\cos \theta - \mu_k \sin \theta)}$$

Check Units

Yup!

$$[N] = [ ] [kg] [m/s^2] \quad \checkmark$$

Better to pull the box 

EXECUTE the PLAN

Calculate Target Quantity(ies)

For Positive Box

$$F_p = \frac{\mu_k m g}{(\cos \theta - \mu_k \sin \theta)}$$

EVALUATE the ANSWER

Is Answer Properly Stated?

NOTE: There is a best angle to pull... and it is not 0°

Is Answer Complete?

Why is Answer Reasonable?

$$m \uparrow \quad F_p \uparrow$$

$$\mu_k \uparrow \quad F_p \uparrow$$

$$\theta \uparrow \quad F_p \uparrow$$

(this is harder to see...  
cos θ ↓ sin θ ↑  
so denominator is getting smaller!

For  $\theta = 0^\circ$

$$F_p = \mu_k m g = (0.3)(70 \text{ kg})(9.8 \frac{m}{s^2}) =$$

For  $\theta = 50^\circ$  (down or push) 206 N

$$F_p = 498 \text{ N}$$

For  $\theta = -50^\circ$  (up or pull)

$$F_p = 236 \text{ N}$$